

Numbers

Complex numbers: $Z = R + iI$, R and I are Real numbers and: $i = \sqrt{-1}$

" R " is the real part and " iI " is the imaginary part. Ex.: $Z = 2 - i3$

1. Real numbers "R": all numbers including "Rational" and "Irrational" numbers as follows.

Rational numbers "Q" is defined as the ratio of $(\frac{m}{n})$, m and n are Integers but $n \neq 0$. $Q \in R$

The ratio can be summarized in one of the following cases:

Ex.: $\frac{-12}{4} = -3$, an integer.

$\frac{19}{8} = 2.375$, an ending decimal.

$\frac{7}{3} = 2.33333 \dots = 2.\bar{3}$, a repeating decimal.

Note: A rational number cannot be an endless decimal, but due to limitation of number of digits in calculators sometimes the end or repeating digits cannot be seen:

$\frac{17}{13} = 1.30769230769$ or $\frac{19}{23} = 0.82608695652$

Natural numbers "N", are whole numbers used for counting: $\{0, 1, 2, 3, 4, 5, \dots\}$. $N \in Z \in Q \in R$

Note: In some sources, Zero is included in Whole numbers "W", but excluded in Natural numbers.

Integers "Z": are positive and negative natural numbers, $Z = +/ - \{N\}$. $Z \in Q \in R$

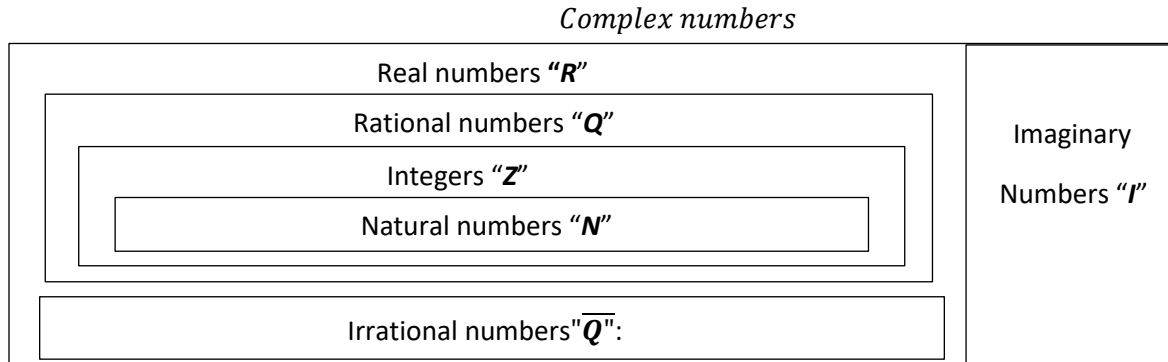
Irrational numbers " \bar{Q} ": or Q' : are endless decimals, it happen in the case of "not perfect root". $\bar{Q} \in R$

Ex.: $\sqrt{5}$, $\sqrt[3]{4}$, this set also includes " π " = 3.14159265359 and " e " = 2.71828182846 (natural log base).

Transcendental numbers; π and e , means they are not a solution of an algebraic equation

Ex.: $x^2 - 5 = 0$ in which: $x = \mp\sqrt{5}$

Numbers are summarized in the following diagram:



2. Imaginary numbers: are the square root of a negative number which will be treated with 2 separate factors: $\sqrt{-1}$ represented by "i" and a real number "I"

Ex.:
$$Z = 3 + \sqrt{-2} = 3 + i\sqrt{2}$$

Notes:

$i = \sqrt{-1}$	$i^2 = -1$
$i^3 = -1i = -i$	$i^4 = +1$

Prime Numbers:

Are natural numbers which are only divisible by 1, and themselves, means their only factors are 1 and themselves. 0, 1 are not a prime number.

Ex. {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 91, 97, }

Factorial:
$$n! = 1 \times 2 \times 3 \times 4 \times 5 \times \dots \times (n - 2) \cdot (n - 1) \cdot n$$

Ex.: $6! = 1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 = 720$